

Offshore Wind Turbines

ITTC Quality System Manual

Recommended Procedures and Guidelines

Guideline

Uncertainty Analysis for Model Testing of Offshore Wind Turbines

7.5 Process control

- 7.5-02 Testing and Extrapolation Methods
- 7.5-02-07 Loads and Responses
- 7.5-02-07-03 Ocean Engineering

7.5-02-07-03.17 Uncertainty Analysis for Model Testing of Offshore Wind Turbines

Disclaimer

All the information in ITTC Recommended Procedures and Guidelines is published in good faith. Neither ITTC nor committee members provide any warranties about the completeness, reliability, accuracy or otherwise of this information. Given the technical evolution, the ITTC Recommended Procedures and Guidelines are checked regularly by the relevant committee and updated when necessary. It is therefore important to always use the latest version.

Any action you take upon the information you find in the ITTC Recommended Procedures and Guidelines is strictly at your own responsibility. Neither ITTC nor committee members shall be liable for any losses and/or damages whatsoever in connection with the use of information available in the ITTC Recommended Procedures and Guidelines.

Updated / Edited by	Approved
Specialist Committee on Testing of Marine Renewable Devices of the 29 th ITTC	29 th ITTC 2021
Date: 07/2019	Date: 06/2021



Uncertainty Analysis for Model Testing of Offshore Wind Turbines



Table of Contents

1. PUR	POSE OF THIS GUIDELINE3
2. GEN UNC	IERAL GUIDE TO CERTAINTY ANALYSIS3
2.1 St	andard uncertainty3
2.2 Co	ombined standard uncertainty4
2.3 Ex	xpanded uncertainty (U)5
3. SOU TES	RCES OF UNCERTAINTY FOR TING OWT5
3.1 M	odel5
3.1.1	Rotor nacelle assembly and tower 5
3.1.2	Substructure6
3.1.3	Stationkeeping system6
3.1.4	Foundation6
3.1.5	Numerical model7
3.2 M	odel installation7
3.3 Co	ontrol systems and actuators7
3.3.1	Variable speed control7
3.3.2	Blade pitch controller7
3.3.3	Required actuators8
3.3.4	Hybrid testing8
3.4 M	easurement and data processing8
3.4.1	Measurement sensors8
3.4.2	Time duration and realization of extreme events9
3.4.3	Data acquisition9
3.4.4	Postprocessing9
3.5 Er	vironmental condition modelling 9
3.5.1	Physical properties10
3.5.2	Waves10
3.5.3	Wind10

3	.5.4	Current	11
3	.5.5	Numerical model	11
3.6	Ini	tial test conditions	11
3.7	Otl	ner sources of uncertainties	12
3	.7.1	Scaling effects	12
3	.7.2	Human factors	12
4 F	EX A I	MPLE OF UNCERTAINTY	
A	NA]	LYSIS TO OFFSHORE WIN	ND
T	TURI	BINE MODEL TEST	12
4.1	Exj	perimental model	12
4.2	Reg	gular Wave Test	15
4.3	Ber	nding moment RAOs	16
4.4	Tyj	pe A Uncertainty	16
4	.4.1	Waves	16
4	.4.2	Assessment of Type A uncert	tainty
			18
4.5	Tyj	pe B Uncertainty	18
4	.5.1	Temperature and Density	18
4	.5.2	Wave gauges	19
4	.5.3	Strain gauges	19
4	.5.4	Geometry and Inertia of	10
		Experimental Model	19
4	.5.5	Bending moment RAO	19
4.6	Sin	nplified semi-analytical	10
	uno	certainty propagation	19
4.7	Tot	tal Type B Uncertainty	20
4.8	Tot	tal Uncertainty	21
4.9	Co	nclusions	21
5. F	REFI	ERENCES	22

Uncertainty Analysis for Model Testing of Offshore Wind Turbines



1. PURPOSE OF THIS GUIDELINE

The purpose of the guideline is to provide guidance on the application of uncertainty analysis to the model scale testing of offshore wind turbines following the ITTC Procedure 7.5-02-07-03.8, "Model Tests for Offshore Wind Turbines". The model scale testing of offshore wind turbines focuses on the environmental loads and global response of the structure, similar to the testing of other offshore structures (floating or fixed).

The uncertainty analysis should be performed following the ITTC Procedures 7.5-02-01-01, "Guide to the Expression of Uncertainty in Experimental Hydrodynamics" (ITTC 2014a), 7.5-02-02-02, "General Guidelines for Uncertainty Analysis in Resistance Tests" (ITTC 2014b), and 7.5-02-01-07, "Guideline to Practical Implementation of Uncertainty Analysis" (ITTC 2017). These guidelines are based on the comprehensive International Organization for Standardization (ISO) Guide to the Expression of Uncertainty in Measurement, also called JCGM (2008). The following procedure adapts the same notation and definitions as provided in ITTC Procedure 7.5-02-01-01 "Guide to Expression of Uncertainty in Experimental Hydrodynamics" (ITTC2014a).

2. GENERAL GUIDE TO UNCER-TAINTY ANALYSIS

The aim of an uncertainty analysis is to provide a quantitative measure of how reliable (or to what level of precision) a measurement is. According to JCGM (2008) the uncertainty of measurement can be defined as the "parameter, associated with the result of a measurement, that characterizes the dispersion of the values that could reasonably be attributed to the measurand." Uncertainty should be differentiated from "error"- which relates to incorrectly setting up the experiment or analysis: doing a mistake.

The uncertainties can be classified into three categories (JCGM, 2008): Standard uncertainty, combined standard uncertainty, and expanded uncertainty. A brief summary of the uncertainty classifications is provided below.

2.1 Standard uncertainty

The standard uncertainty (u) is the uncertainty of the result of a measurement expressed in terms of a standard deviation. The standard uncertainty can be grouped into two types, type A and type B, where the type depends on the method for estimation of uncertainty.

Type A: Uncertainty components obtained using a method based on statistical analysis of a series of observations. The standard uncertainty by type A for a series of *n* repeated samples (or observations) is estimated by

$$u(\bar{q}) = s/\sqrt{n} \tag{1}$$

where s and \overline{q} are the standard deviation and arithmetic mean, respectively, of the samples.

Type B: Uncertainty component obtained by other means (other than statistical analysis). Prior experience and professional judgements are part of Type B uncertainties.

2.2 Combined standard uncertainty

If a measurement result y is obtained from N other measured quantities $x_1, x_2, ..., x_N$, then the standard uncertainty of the result is a combination of the standard uncertainties of the other quantities. This combined standard uncertainty



7.5-02

 u_c is given by the law of propagation of uncertainty, i.e. for a measurement result $y=f(x_1,x_2,...,x_N)$, the combined standard uncertainty is defined as

$$u_{c}^{2}(y) = \sum_{i=1}^{N} c_{i}^{2} u^{2}(x_{i}) + 2\sum_{i=1}^{N-1} \sum_{j=i+1}^{N} c_{i} c_{j} u(x_{i}) u(x_{j}) r(x_{i}, x_{j})$$
(2)

where the sensitivity coefficients $c_i = \partial f / \partial x_i$ and $c_j = \partial f / \partial x_j$ determines how the measurement result varies with changes in these quantities. Furthermore, $r(x_i, x_j)$ is the correlation coefficient and ranges between -1 and +1.

If the input quantities x_i and x_j are uncorrelated, then $r(x_i, x_j)=0$ and the combined standard uncertainty equation (2) reduces to the first summation term only.

Categories	Sources	Examples (related to all sources)
Model	Rotor nacelle assembly, tower and substruc-	Mass properties, geometry,
	ture	structural elasticity
	Stationkeeping system (only floating)	Restoring forces
	Foundation (only bottom-fixed)	"Soil" stiffness and damping
	Numerical model (if applicable)	Numerical approximation
Model instal-	Ballasting and trimming (only floating)	Reading of trimming
lation	Positioning and alignment	
Control sys-	Variable speed control	Tip-speed ratio
tems and actu-	Blade pitch control	Blade pitch angle
ators	Actuators	
	Hybrid testing (if applicable)	Achievement of target aerody-
		namic loads
Measurement	Measurement sensors	Accuracy
and data pro-	Test duration and realization of extreme events	
cessing	Data acquisition	Precision
	Postprocessing	
Environmen-	Non-controlled physical properties	Temperature, density, viscosity
tal condition	Waves	Wave spectra
modelling	Wind	Wind spectra
	Current	Current turbulence
Initial test	Mooring lines (only floating)	Mooring layout
conditions	Time between two consecutive tests	Remaining turbulence and fluid
		circulation
Other	Scaling effects	Reynolds vs Froude scaling

Table 1: U	Uncertainty	categories	and	sources
------------	-------------	------------	-----	---------



2.3 Expanded uncertainty (U)

The expanded uncertainty $U=ku_c(y)$ is introduced to provide an interval about the measurement result that may be expected to encompass a large fraction of the distribution of values that could reasonably be attributed to the measurand *Y*. The numerical value for the coverage factor *k* should be chosen so that the interval $Y = y \pm U$ corresponds to a particular level of confidence. This factor usually corresponds to 95% confidence.

For most hydrodynamic tank experiments, the Student *t*-distribution may be assumed for a small number of observations (cf. Figure 1 in ITTC, 2014a). For a large number of degrees of freedom (v = n-1>30), the distribution may be assumed to be Gaussian with a coverage factor of k=1.960.

3. SOURCES OF UNCERTAINTY FOR TESTING OWT

A first step in uncertainty analysis is to identify all significant sources of uncertainty. The sources of uncertainty related to model testing of offshore wind turbines can be grouped into these main blocks: model, installation, control system and actuators, measurement and data processing, environmental condition modelling, and initial test conditions.

In the following sections the various sources of uncertainties are discussed, and a summary is provided in Table 1. Unless specified, each source should be considered relevant both for fixed and floating offshore wind turbines.

3.1 Model

Uncertainty sources related to the model (the test object) are mainly a result of tolerances in manufacturing and deformation occurred after manufacturing (e.g. during installation and model testing). These steps create uncertainties in the model geometry, the inertial properties, and structural elasticity and damping. Furthermore, if numerical simulations are necessary in order to prepare or perform the experiments, there will be sources of uncertainties associated with the numerical model.

Offshore wind turbines usually comprise of the following parts: The rotor and nacelle assembly (RNA), tower, substructure (floating or bottom-fixed), stationkeeping system (floating) or sea-bed foundation (bottom-fixed).

Uncertainty sources related to the model are outlined below.

3.1.1 Rotor nacelle assembly and tower

The rotor nacelle assembly (RNA) represents a considerable source of uncertainty (Robertson, 2017). The blade geometry, pitch setting, mass distribution, structural damping and stiffness are the most significant sources. Manufacture of a rotor with the correct mass properties and adequate stiffness can prove very challenging. The complexity of the blade geometry and its influence on the turbine loading represent a significant uncertainty in the measured loads from the definition of the RNA model.

The tower stiffness, structural damping, mass distribution and its connection to the RNA and substructure represent other sources of uncertainty. The tower is often connected to the RNA and substructure through load cells. This may add additional compliance to the system and is another source of uncertainty.

iπ	ITTC – Recommended Procedures and Guidelines	7.5-02 -07-03.17 Page 6 of 23		
INTERNATIONAL TOWING TANK CONFERENCE	Uncertainty Analysis for Model Testing of Offshore Wind Turbines	Effective Date 2021	Revision 00	

For a fully instrumented physical rotor model, it may also be difficult to achieve the scaled-down mass (Gueydon, 2016), especially for smaller model scales. This can be accounted for by shifting masses in the support structure to maintain the global moments of inertia and COG, but the mass distribution will not be maintained which is of importance for force measurements and structural modes for elastic towers.

3.1.2 Substructure

Uncertainties in the substructure will come from the geometry, mass distribution and stiffness properties. Distortion of geometry may affect the displaced volume and waterplane area, both affecting the hydrostatic properties and hydrodynamic loading. Furthermore, the surface roughness and sharp/rounded corners/edges may affect viscous damping.

Uncertainty in the mass distribution affects the inertia properties of the floater as well as the centre of mass. Stiffness properties of flexible members and joints may also be a source of uncertainty.

Small water absorption or deformation due to hydrostatic pressure can influence the model draught and mass distribution, being another source of uncertainty.

3.1.3 Stationkeeping system

The purpose of a stationkeeping system is to limit the horizontal excursions and maintain orientation of floating wind turbines. The type of stationkeeping system depends on the type of floater, and typically it comprises of mooring lines and anchors, tendons anchored to sea bottom, and/or active thrusters (DP-system). The latter is less relevant for offshore wind turbines. As for mooring lines and tendons it is important to maintain the correct line characteristics. Uncertainties relates especially to the difficulty to scale the axial stiffness (EA) distribution and the mass distribution in the same time (Qui et al., 2014). This often leads to partial or total replacement of original segments with additional spring elements, and clump weights and/or buoyance elements to correct submerged weight.

Other sources of uncertainty that influence the line characteristics include fairlead position, line segments length and diameter, line pretension, anchor positions, and sea-bottom friction. In-line load cells used to measure line tension may also alter the properties of the lines and tendons.

In the case where it is required to model a mooring system consisting of synthetic fibre ropes – the large sensitivity to extreme mooring loads of the material should be taken into account to correctly reproduce the stress-strain characteristics. Dynamic characteristics of the synthetic ropes should also be considered.

Truncation or other simplifications of the mooring lines may lead to other distortions, and in some cases to a totally different mooring system than originally specified (Qui et al., 2014). It is important to maintain correct geometrical parameters such as top angles and lines elongation during excursion. Uncertainty analysis should be conducted to determine the degree to which the restoring characteristics have been achieved and to allow this effect to be included in an analysis of the overall model test.

3.1.4 Foundation

For bottom-fixed wind turbines, the soil stiffness and damping cannot be neglected due



to its influence on the global response. Typically, the foundation is modelled by a "soil spring" extended down to the foundation. This connection should be designed to give realistic stiffness, but also damping for cases when aerodynamic damping is low. The imperfection and/or simplification of the soil model is a source of uncertainty.

The bottom stiffness may also be an uncertainty if the foundation is not rigidly fixed to the ground. The force transducer at the base of the wind turbine may also alter the stiffness of the foundation as well.

3.1.5 Numerical model

Numerical simulation models may constitute an important part of a test object, either in redesign of the model due to limitations when scaling down the structure (e.g. performance scaling of rotor blades, truncation of mooring lines) or as a replacement of a physical substructure by numerical simulations and actuators (e.g. hybrid testing).

Sources of uncertainties in the numerical modelling can be caused by e.g. choice of mathematical model to describe real physics, introduction of empirical parameters, choice of numerical method, grid and timestep resolution, numerical accuracy and convergence criteria, computing capacity and simulation time, among others.

3.2 Model installation

Installation uncertainty sources relates to hull model ballasting and trimming, model positioning and alignment relative to wave maker and wind generator, mooring and anchor layout (including mooring line pretension and top angle), fastening of bottom fixed structures, and so forth. Another source of installation uncertainty may relate to deformation of the model due to brute force from manual labour when moving or fixing the model.

3.3 Control systems and actuators

There are model parameters necessary for control design to ensure that the controller does not introduce any destabilizing dynamic system behaviour that would lead to excessive and unrealistic loads above rated operating conditions: aerodynamic coefficients (power and thrust), drivetrain mass, inertia, platform surge/pitch eigenfrequency, platform surge/pitch damping, platform mass/inertia, platform hydrodynamic coefficients, quasi-static mooring lines, wind turbine mass/inertia, tower elasticity, blade elasticity, blade polars, yawed inflow, aeroelastic stability, 3D gyroscopic effects and others.

3.3.1 Variable speed control

From cut-in wind speed to rated wind speed the rotor speed varies in order to allow for an optimal power production. Thus, the optimal tip-speed ratio *TSR* is tracked by controlling the rotor speed Ω with the generator torque at all operating wind speeds v_0 : $TSR=\Omega R/v_0$. No negative damping effect arises for below-rated wind speeds since the thrust is increasing with increasing wind (Jonkman 2007). For variable speed control, the uncertainty relates to the actual rotor speed Ω .

3.3.2 Blade pitch controller

The most critical control region is the region above rated wind speeds, where the collective blade pitch controller is active to keep the generator torque and rotor speed constant. A PIcontroller is the standard way. The dynamics including the controller and the closed feedback



loop of rotor speed to blade pitch angle is referred to as "closed-loop dynamics". In order to keep the closed-loop system dynamics constant throughout all operating points above rated conditions, a method called "gain scheduling" is necessary. For floating wind turbines especially this above-rated control is critical since the pitching of the blades can destabilize the floating wind turbine system. Uncertainty analysis should be conducted on the gain scheduling in order to determine the degree to which the target blade pitch angle has been achieved.

3.3.3 Required actuators

The actuators for modern wind turbines control the three blade-pitch angles and the generator torque. The blade pitch actuators can be independent of each other to allow for individual pitch control (IPC). This accounts for azimuthdependent wind loads and reduces the blade and tower-top fatigue loads. Usually a brushless motor is used to control the turbine rotation speed and torque in water basin model tests. The driving torque is measured by a torque sensor. The type B uncertainty of motors and torque meters is estimated by the manufacturer's specifications.

3.3.4 Hybrid testing

In hybrid testing where the aerodynamic loads on the blades are simulated and imposed by actuators or a passive mass or a disc, uncertainty analysis should be conducted as per ITTC recommended Procedure (7.5-02-01-01, Guide to Expression of Uncertainty in Experimental Hydrodynamics) to determine the degree to which the target wind load characteristics have been achieved and to allow this effect to be included in an analysis of the overall model test.

3.4 Measurement and data processing

Wave, current, wind, model motions, rotor rpm, generator rpm, shaft torque, generator torque, power, bending moments, accelerations and relative motions, etc. are the primary measurements in water basin model tests. All parameters are subjected to type A and type B uncertainties. Type A uncertainty is evaluated based on repeated measurements and type B uncertainty is not revealed by repetition of the experiment. Type B sources of uncertainty include the geometry of used models, measurement sensors, the calibration and installation of equipment, data acquisition systems, data processing, etc.

3.4.1 Measurement sensors

It is very important to ensure that the instrumentation used in test set-up have the required properties. Common sensors mainly used for measurement are the followings: Real-time optical tracking system, loadcell (i.e. 6-axis, oneaxis, ring-type, etc.), torque meter, mooring line tension meter, wave probe, anemometer, current speed meter, thermometer, accelerometer, pressure gauge, strain gauge, inclinometer, leveller, electric weight scale, LVDT, electric current meter, etc. Specifications provided by sensor manufacturers and previous experience with sensors allow for the estimate of type B uncertainties.

Sensors are often affected by the temperature. For slow variations in temperature this can introduce drift in the measured signal. This can be controlled by making a zero reading. When a pressure gauge hits the water, the temperature changes abruptly due to the difference in air and water temperature. Temperature change occurs at the same time as the impact pressure change and then direct use of the measured signal can give totally misleading results (Steen, 2014).



Careful calibration procedures are important to minimize measurement uncertainty. Generally, in-situ end-to-end calibration includes as many elemental uncertainty sources in the system as possible which do not have to be identified or individually estimated. Also, calibration standard, calibration misalignments, calibration curve fitting and A/D conversion are considered in the estimate of uncertainty. The curve fitting uncertainty can be estimated using the standard deviation of estimate formula. (ITTC procedure 7.5-02 07-02.1 Rev.4, 2011) The type B uncertainty of A/D conversion is equal to half of resultant resolution.

Some measurements require the presence of cables attached to the RNA, and these may be a source of uncertainty for the mass, moments of inertia, aerodynamic loads, and damping. Careful calibration methodology must be followed to properly quantify the effect of the cables (e.g. decay test with and without cables).

3.4.2 Time duration and realization of extreme events

Realizations of combined environments in water basins require different time durations depending on load cases to be stochastically valid: 10-minutes under wind and regular waves for effective RAOs, 1-hour under wind and irregular waves for operating conditions or 3-hours under wind and irregular waves for extreme events with initial transient periods. All of the time durations above are in full scale. Specially, the properties of short and steep waves may change downstream, and the wave measurements should be carried out along the entire test track during wave calibration. Also, the shape of the irregular wave spectrum is an important uncertainty source and it is required to ensure the measured spectrum shape agrees with the theoretical shape.

Due to numerical simulation limitation and/or ocean basin limitation different combinations of durations and number of seeds are used for the wind and wave realizations. The uncertainty of the wind and wave extreme values depends on the selected approach.

3.4.3 Data acquisition

A typical data acquisition system consists of a signal conditioner, Analog-to-Digital Converters (ADCs), and computer bus. Signal conditioning includes amplifying, filtering, smoothing, etc. When in-situ end-to-end calibration procedure is applied, all the data acquisition system elemental uncertainty sources are included in the process except for the noise. Both sampling rate and bit resolution are considered in selecting ADC and its uncertainty can be estimated by processing a known signal with a known analytical solution (i.e., sine).

3.4.4 Postprocessing

Postprocessing includes collection of measured data, data filtering, digitization of analog signals including peaks, reduction to a non-dimensional format, regression on the test data to acquire a mathematical fit, calculation of RAOs, spectrum, exceedance probability, stochastic averages (pdf, cdf, joint pdf, mean, standard deviation, significant value, etc.) and long-term prediction with 50 to 100 year extreme values using the generalized extreme values distribution (i.e. Gumbel & Weibull, etc.). The type B uncertainty should be included.

3.5 Environmental condition modelling

The uncertainties associated with the environmental condition modelling are related to multiple sources: the physical properties of the testing environment (e.g. air and water temperature and density, bottom friction, etc.), and the



physical properties of the generated environment characteristics (e.g. wind, waves, and currents).

3.5.1 Physical properties

Some of the environmental physical properties that are important sources of uncertainty but that are not necessarily controlled are: air density and temperature, water density and temperature, ocean basin floor friction, and water depth.

These uncertainties are linked to the accuracy of the instruments used to measure them, and to their variability over the time and space scales of the test – which may require repeat measurement in different points (space scale) and at different times (time scale) to reduce the uncertainty.

If controlled (e.g. moving floor to achieve desired water depth), the limitations of the control system, such as accuracy and repeatability, constitute an additional source of uncertainty.

3.5.2 Waves

A second source of uncertainty is the temporal and spatial variability of the generated waves, and its significance is related to how well the measuring system used captures these variabilities.

From a temporal point of view, wave reflection may be a source of uncertainty.

From a spatial point of view, for example, if the water surface elevation is measured only in one or few points of the tank, uncertainty on the actual surface elevation in other points may arise. Guidelines on where to measure these characteristics are given in the ITTC Recommended Procedure 7.5-02-07-03.1 "Floating Offshore Platform Experiments" (ITTC 2017a). Another spatial uncertainty may be the wave kinematics variability with depth, if these characteristics are measured only at one water depth – this is even more important when shallow water conditions are present. Incorrect boundary conditions can also lead to low frequency parasitic waves as an additional source of uncertainty.

Furthermore, a type A source of uncertainty is related to the inherent stochasticity of irregular waves over time. Repeated measurements can reduce this source of uncertainty.

3.5.3 Wind

An important source of uncertainty originates from the limitations, in terms of accuracy and repeatability, of the physical equipment used to generate wind (for hybrid testing, where the wind is simulated numerically and only wind forces are generated physically, see section "Numerical model" below).

Similar to waves, important spatial and temporal variabilities characterize a generic turbulent wind acting on an offshore wind turbine model, and the magnitude of these uncertainties is linked to in how many points (spatial) and how often (temporal) a measurement of the wind speed is taken.

For example, from a spatial point of view, even measurements taken in multiple points across the wind rotor plane (2-D) would not capture the wind velocity and wind turbulence variability in a plane perpendicular to the rotor plane – which can be significant for a floating offshore wind turbine system, as noted by Robertson (2017). Wind-wave interaction and wind blockage are other sources of wind spatial and temporal variability.



The temporal variability of wind speed and turbulence may also be an important source of uncertainty.

Furthermore, a type A source of uncertainty arises when testing in turbulent wind conditions, due to the inherent stochasticity of turbulence. Repeated measurements can reduce this uncertainty.

3.5.4 Current

The limitations, in terms of accuracy and repeatability, of the physical equipment used to generate the current is a primary source of uncertainty.

As for waves and wind, the impact of the spatial variability of current velocity and turbulence on uncertainty should be assessed by measurements made at multiple points, both across the horizontal plane and the vertical water column.

In addition, turbulent currents are inherently stochastic, leading to a type A uncertainty. Repeated measurements can reduce this uncertainty.

3.5.5 Numerical model

As reported by the ITTC Recommended Procedure 7.5-02-07-03.8 "Model Tests for Offshore Wind Turbines" (ITTC, 2017b), hybrid testing refers to "methods that combine, in real time and interactively, the numerical simulation of a virtual substructure with a physical substructure tested experimentally in model scale."

As such, the additional uncertainty sources to be considered in this case are linked to two factors: the numerical simulation model, and the physical equipment used to "convert" the forces calculated numerically into physical forces acting on the physical substructure.

As every numerical model, the numerical simulation used is a simplification of the real phenomenon, and therefore a source of uncertainty is the accuracy with which it reproduces it. Usually, the physical wind and forces acting on the rotor are emulated, respectively, by a synthetic (numerically generated) wind speed and a numerical aerodynamic model deriving the forces transmitted by the rotor to the wind turbine tower at model scale. Therefore, in this case, the uncertainty is linked to the accuracy of the numerical approaches used to reproduce the wind spatial (e.g. wind shear) and temporal (e.g. turbulence) variability, and to the accuracy of the numerical approach used to calculate the wind forces acting on the rotor. For example, usually Blade Element-momentum theorybased are usually used to calculate these aerodynamic forces, due to their relatively low computational cost, but these are known to have several limitations (see, for example, Gupta et al., 2005).

The forces calculated by the numerical simulation are then downscaled and imposed on the physical model through a physical system. Depending on the system (single ducted fan driven by an electronic motor, as in Azcona et al. (2014), or a set of fan see Urban and Guanche (2019). For actuated cables see Sauder et al (2016), Bachynski et al. (2016), and Berthelsen et al (2016), among others). Source of uncertainty are linked to the limitations (accuracy and repeatability) of the components used.

3.6 Initial test conditions

Mooring lines on seabed, hysteresis, remaining waves, circulation, turbulence, current, etc. in water basin are primary uncertainty sources



of initial test set-up and the uncertainties are estimated by the past experiences.

Due to small asymmetry in the model arrangement, a small roll response may occur in head sea and this roll increases when the rotor is in action. (Boulluec et al. 2013). Also diffracted waves and reflected waves due to offshore wind turbine motions will reach to the tank wall and the wave generator and will be reflected back to the model. In this way a transverse wave system will gradually be developed, and the tank wall interference effects can have a very important effect on the experimental results. (Steen 2014, Zhao et al. 1988). Also, the time between two consecutive test cases should be long enough to ensure an acceptable quiescence of water. The type B uncertainty should be estimated by the past experiences.

3.7 Other sources of uncertainties

3.7.1 Scaling effects

For offshore wind turbines, aerodynamic and hydrodynamic loads can be of equal importance when estimating its dynamic response. While for hydrodynamic loads Froude scaling is usually adopted, the aerodynamic forces should be scaled according to Reynolds scaling. The two dimensionless ratios cannot be satisfied at the same time, and usually offshore wind turbine models are Froude scaled. Therefore, the mismatch of Reynolds number is a source of uncertainty for aerodynamic loads that should be considered in the design of the test setup. See ITTC Procedure 7.5-02-07-03.8, "Model Tests for Offshore Wind Turbines" (ITTC, 2017b) for different approaches of modelling the wind turbine. E.g. for performance modelling the blades are redesigned to provide the same thrust and torque in a low Reynolds number different from that in full scale. Uncertainty analysis should be conducted on the redesigned blades in order to determine the degree to which the target wind load characteristics have been achieved and to allow this effect to be included in an analysis of the overall model test.

Additional uncertainty sources due to the scaling, in common with other offshore structures, are viscous effects on the hull (e.g. slender parts, appendages) and mooring lines. See also Qiu et al. (2014).

3.7.2 Human factors

Human factors can be classified as error rather than uncertainty sources. See e.g. Qiu et al. (2014) for further details.

4. EXAMPLE OF UNCERTAINTY ANALYSIS TO OFFSHORE WIND TUR-BINE MODEL TEST

The following example is based on the article: "Dynamic response of a monopile wind turbine in waves: Experimental uncertainty analysis for validation of numerical tools" (Bachynski et al., 2019).

4.1 Experimental model

The prototype design corresponds to the NREL 5MW reference wind turbine (Jonkman et al., 2009), supported by the offshore tower developed in OC3 Phase III (Jonkman, 2010) and a 7 m diameter monopile, with the OC3 Phase II soil stiffness parameters (Jonkman and Musial, 2010). The monopile thickness is 60 mm and the transition from monopile to tower occurs at 10 m above the waterline (Figure 1 and Table 1).



Table 2: Key model particulars, compared to the design prototype and to the OC3 Phase II monopile (Jonkman and Musial, 2010). All values in full scale. Note that the OC3 Phase II monopile is in 20 m water depth, compared to the present model in 30 m water depth.

	Model Tests	Prototype	OC3 Phase II Monopile
Diameter(wetted section of monopole) [m]	7.0	7.0	6.0
Tower baase diameter (10 m above waterline) [m]	6.5	6.5	6.0
Tower top diameter [m]	3.87	3.87	3.87
RNA mass [kg]	3.36x10 ⁵	3.50 x10 ⁵	3.50 x10 ⁵
RNA Ixx about RNA CoG [kg m ²]	7.14x10 ⁷	4.00×10^7	4.00×10^7
RNA Iyy about RNA CoG [kg m ²]	7.14x10 ⁷	3.07x10 ⁷	3.07x10 ⁷
RNA Izz about RNA CoG [kg m ²]	9.51x10 ⁷	2.44×10^7	2.44×10^7
Monopile penetration depth (below seabed) [m]	-	46	30





Figure 1: Sketch of the monopile model, without (left) and with (right) outer shells

iπ	ITTC – Recommended Procedures and Guidelines	7.5-02 -07-03.17 Page 15 of 23	
INTERNATIONAL TOWING TANK CONFERENCE	Uncertainty Analysis for Model Testing of Offshore Wind Turbines	Effective Date 2021	Revision 00



Figure 2: Left: photograph of the model installed in the wave basin, highlighting the drag disk. Right: numerical model in SIMA, where the four upper lines represent the drag disk. Transition from red to black checkerboard indicates the calm water free surface

The model tests were carried out at a scale 1:40 in the Ocean Basin at SINTEF Ocean (Figure 2). Froude scaling (including the difference between the fresh water density in the model tests and sea water density at full scale) is applied in order to scale the model test results.

4.2 Regular Wave Test

As shown inTable 3, 9 regular waves were tested, with periods (T) ranging from 6 to 14 seconds. The steepness-value was considered (approximately 1/30). The Keulegan-Carpenter (KC) number, defined in Eq.1, for all of the considered tests is quite low. For the smallest waves (KC < 1.25), no flow separation is expected



(Sarpkaya and Isaacson, 1981), and for KC up to 5.0, the added mass coefficient is not expected to vary significantly (DNV, 2010). In Table 3, the KC number for regular waves is calculated, based on the maximum velocity according to linear theory by Equation (1): where U_{max} is the maximum water particle velocity, perpendicular to the monopile axis, at water surface level, *T* is the wave period, *H* is the regular wave height, *k* is the wave number, *h* is the water depth, and *D* is the diameter of the monopile (characteristic length).

$$KC = \frac{U_{max}T}{D} = \frac{\pi H_1}{\tanh(kh)D}$$
(1)

Table 3: Regular wave tests (full scale).

<i>H</i> [m]	1.9	2.6	3.3	4.2	5.2	6.3	7.5	8.8	10.2
<i>T</i> [s]	6.0	7.0	8.0	9.0	10.0	11.0	12.0	13.0	14.0
KC	0.85	1.18	1.54	2.04	2.65	3.39	4.27	5.31	6.50

4.3 Bending moment RAOs

The bending moment transfer function $R(\omega)$, denoted as the response amplitude operator (RAO) of the bending moment at z = -28.5 m, for the first harmonic of the primary wave frequency for wave periods 6 s, is defined in Eq. 2:

$$R(\omega) = M y_1 / \eta_1 \tag{2}$$

Where My_1 is the amplitude of the first harmonic bending moment, and η_1 is the amplitude of the first harmonic wave.

4.4 Type A Uncertainty

Type A uncertainties are evaluation of uncertainty by the statistical analysis of a series of observations (JCGM (2008) and Taylor et al. (1993)). This type of uncertainty is as also commonly known as the precision uncertainty of the test. Repeatability is assessed directly from the experimental results.

4.4.1 Waves

Assessing the repeatability of the RAO is challenging for several reasons. The generation of regular waves in relatively shallow water can be challenging due to the depth variations and reflections, standing waves, and parasitic waves in the basin.

There were 13 standing probes (present during both the calibration and the tests with the model) and 23 probes along a wave harp (a set of tightly-spaced wave probes aligned with the wave propagation direction, with a distance of 6 m between each probe and connected to a single support), which was only present during wave calibration. The wave harp is shown in Figure 3.





Figure 3: Wave probe layout during calibration of long-crested waves. Right: zoom near the model, showing the tightly-spaced wave probes in the harp (a set of tightly-spaced wave probes aligned with the wave propagation direction).



Figure 4: Variations in regular wave amplitude along the wave harp. Left: amplitude of the first harmonic of the wave along the harp, where WAVE2 shows the value at the model location. Note that the indicated steepness 1/30 and 1/40 are approximate. Middle: time series of wave elevation along the harp (T = 6 s, lower steepness). Right: time series of wave elevation along the harp (T = 13 s, lower steepness).





Figure 5: Experimental bending moment (at z = - 28:5 m) RAO results, highlighting the repeatability and the differences in results for different wave steepness

There are notable differences in the amplitude of the first harmonic of the wave, especially for the longest waves (Figure 4). Type A uncertainty of bending moment transfer function was:

$$s_R = 0.354E + 05 \text{ Nm/m}$$

4.5 Type B Uncertainty

Type B uncertainties are the evaluation of uncertainty by means other than statistical analysis (JCGM (2008) and Taylor et al (1993)). These are also commonly known as bias uncertainties.

4.5.1 Temperature and Density

The temperature was measured to be 16 0 C , and the temperature variations during the model tests were ±0.07 0 C. Based on the manufacturer data, the temperature error-is 0.03 % per 0 C: considering temperature variations of ±0.07 0 C, the temperature contribution to the Type B uncertainty is negligible compared to the previously described contributions. By applying the method outlined in the water properties ITTC Procedure 7.5-02-01-03, "Density and Viscosity of Water", the density (ρ) is 999.072 kg/m³ and

The wave amplitude at a given location along the harp deviates up to 18 % compared to the mean amplitude, and the coefficient of variation ranges from 3 to 9 % depending on the wave period.

4.4.2 Assessment of Type A uncertainty

Type A uncertainty of a response which is measured repeatedly is found from Equation (3):

$$s_R = \frac{s_x}{\sqrt{N-1}} \tag{3}$$

where s_x is the standard deviation of the measured quantity over *N* repeated tests.

There is a good agreement in the first harmonic RAO for longer waves as shown in Figure 5. The repeated tests also showed good agreement (within 2 %) for the first harmonic. The discrepancies between the results for the different wave steepness were large, but the repeatability of each condition was within 5 %.



Effective Date Revision 2021 00

the corresponding Type B Uncertainty is 0.0306 kg/m^3 .

4.5.2 Wave gauges

The wave gauges have a sensitivity of 2 % / ⁰C. Temperature effects had a relatively small contribution to the Type B uncertainty for the wave gauges.

4.5.3 Strain gauges

Calibration of the strain gauges is carried out by applying a known moment (via a hanging weight attached through a pulley at a given height). We estimated the Type B uncertainty by considering ± 2 mm model scale error in height and ± 5 ^oC uncertainty in orientation of the load applied for calibration.

4.5.4 Geometry and Inertia of Experimental Model

Possible Type B uncertainties in manufacture of the experimental model are estimated in Table 4 and propagated to the responses of interest using a simple semi-analytical model.

Table 4: Estimated Type B uncertainties. All values given in full scale

Parameter	Type B uncertainty			
Measured wave ele-	$\pm 3\%$			
vation				
Water depth	± 0.4 m			
Mass distribution	± 10 % locally			
Inner core dimensions	$\pm 4 \text{ mm}$			
Outer core dimen-	$\pm 6 \text{ cm}$			
sions				
Strain	± 0.5 %			
Acceleration	Orientation $\pm 2.5^{\circ}$,			
	location 0.12 m			

4.5.5 Bending moment RAO

The uncertainty in these response metrics, i.e. bending moment RAO, will depend on the uncertainty in the incoming waves, the model itself (i.e. geometry, stiffness, mass distribution), and the measured response (bending moment) as in Table 5.

Table 5: Independent input variables for semi-analytical analysis

Input varia- ble	Symbol	Comments
Mass distri- bution	т	Affects modal pa- rameters. Uniform relative variation 10 %
Stiffness distribution	EI	Affects modal pa- rameters. Uniform relative variation 4 %
Modal damping	b _i orζ	Varied for all five modes simultane- ously 20 %
Outer diam- eter	D	Only affects wave loads, 6 cm
Water depth	h	Affects modal pa- rameters and wave loads, 0.4 m
Regular wave period	$\frac{2\pi}{\omega}$	affects wave loads, 0.05 s

4.6 Simplified semi-analytical uncertainty propagation

A simplified model is used to propagate Type B uncertainties in the properties of the physical model and in the incoming waves to the bending moment response. This linearized model is obtained by combining a 5-mode structural response model with linear wave loads. The structural response model takes the form of the decoupled ordinary differential equations in Equation (4) through (7), where $\overline{m_i}$ is the modal mass, $\overline{b_i}$ is the modal damping, $\overline{k_i}$ is the modal



Uncertainty Analysis for Model Testing of Offshore Wind Turbines Effective Date Revision

2021 00

stiffness, \overline{F}_i is the modal force, and y_i is the modal response.

$$\overline{m_{i}}\ddot{y_{i}} + \overline{b_{i}}\dot{y_{i}} + \overline{k_{i}}y_{i} = \overline{F_{i}}, i = 1, \dots, 5$$

$$(4)$$

$$\overline{m_i} = \int_{z_{low}}^{z_{top}} m(z)(\varphi_i(z))^2 dz + \sum M_j (\varphi_i(z_j))^2 + \sum I_j (\varphi_{i,z}(z_j))^2$$
(5)

$$\overline{k}_{l} = \int_{z_{low}}^{z_{top}} EI(z)(\varphi_{i,zz}(z))^{2} dz$$
(6)

$$\overline{b}_{l} = 2\overline{m_{l}}\,\omega_{0,l}\,\zeta = 2\zeta\sqrt{\overline{k_{l}}\,\overline{m_{l}}} \tag{7}$$

The undamped natural frequencies obtained from the estimated modal mass and stiffness were found to be within 5 % of those from the eigenvalue analysis. For simplicity, the modal damping is chosen to give the same damping ratio in all five modes. Based on the decay tests, ζ = 0.5 % critical damping is chosen.

In the modal response model, the viscous drag term of the Morison equation was not considered due to the relatively low KC number of the experiments as in Table 3. Then the Morison inertia load takes the form as in Equation (8):

$$\overline{F}_{i} = \int_{-h}^{0} \varphi_{i}(z) \rho(C_{a}+1) \pi \frac{D^{2}}{4} a dz \qquad (8)$$

with *a* for regular waves with amplitude η_a and frequency $\omega = 2\pi/T$ in water depth *h* given by Equation (9):

$$a = \omega^2 \eta_a \frac{\cosh(k(z+h))}{\sinh(kh)} \cos \omega t$$
(9)

According to this simple semi-analytical model, the first response metric, the first harmonic bending moment RAO at $z_j = -28.5$ m, is given by Equation (10).

$$\frac{|H(\omega)| = \frac{|M|z_j|}{|\eta_a|} = \sum_{i=1}^n EI(z_j) \varphi_{i,zz}(z_j) *}{\frac{\int_{-h}^0 (C_a+1)\pi \frac{D^2}{4} \rho \omega^2 \frac{\cosh(k(z+h))}{\sinh(kh)} \varphi_i(z) dz}{\overline{\kappa_i} \sqrt{((1-\beta_i^2)^2+(2\zeta_i\beta_i)^2}}}$$
(10)

In Equation (11), β_i is the frequency ratio for each mode.

$$\beta_i = \frac{\omega}{\omega_i} = \frac{\omega\sqrt{\overline{m_i}}}{\sqrt{\overline{k_i}}} \tag{11}$$

4.7 Total Type B Uncertainty

ī

ı.

To compute the total Type B uncertainty in the measured response u_R , we combine the effects of the inputs in Table 4 with the effects of the estimated bias uncertainties in the wave elevation and bending moment measurements.

Considering a result R which depends on L independent variables x_i , the sensitivity index θ_i is given by Equation (12):

$$\theta_i = \frac{\partial R}{\partial x_i}, \quad i = 1, 2, \dots, L$$
(12)

and evaluated at either mean or nominal values of the result.

The uncertainty in the result due to the Type B uncertainties is obtained by the square root of the sum of squares (RSS) of the contributions from all of the independent variables by Equation (13):

$$u_{R} = \pm \sqrt{\sum_{i=1}^{L} (\theta_{i} u_{x_{i}})^{2}}$$
(13)

Where u_{xi} is the best estimate of the uncertainty in the independent variable.

The most important components of Type B uncertainty of bending moment transfer function $R(\omega)$ at T = 6 s are the wave elevation, mass, and diameter as in Equation (14):



Uncertainty Analysis for Model Testing of

Offshore Wind Turbines

(14)

Page 21 of 23

$$R(\omega) = RAO = \frac{M_y}{\eta_y} = f(m, EI, \zeta, D, h, T, M_y, \eta_a)$$

A calculation in wave period, T = 6 s is made by Equation (15), referring to the values in Table 6.

Table 6: Sensitivity indexes and independent variable uncertainty values

Variable x_i	$\boldsymbol{\theta}_{x_i}$	Units for $oldsymbol{ heta}_{x_i}$	u_{x_i}	Units for $oldsymbol{u}_{oldsymbol{x_i}}$	$\theta_{x_i} u_{x_i}$	Units for $oldsymbol{ heta}_{x_i} oldsymbol{u}_{x_i}$
М	2 55E+03	Nm/(mkø/m)	203 5	ko/m	5 19E+05	Nm/m
FI	4.505.05	N ((N ²)	5.005.00	N 2		
LI G	4.70E-05	Nm/(mNm)	5.60E+09	Nm	2.63E+05	Nm/m
ζ	7.30E+05	Nm/m	0.001	-	7.30E+02	Nm/m
D	7.03E+06	Nm/m ²	0.06	m	4.22E+05	Nm/m
h	2.74E+04	Nm/m ²	0.4	m	1.10E+04	Nm/m
Τ,	9.12E+06	Nm/(ms)	0.05	s	4.56E+05	Nm/m
M_{y}	1.05E+00	Nm/(mNm)	116,840.5	Nm	1.23E+05	Nm/m
η_a	2.51E+07	Nm/m ²	0.0285	m	7.16E+05	Nm/m

 $\int_{R}^{R} = \int_{R}^{R} (\theta_{m}u_{m})^{2} + (\theta_{EI}u_{EI})^{2} + (\theta_{\zeta}u_{\zeta})^{2} + (\theta_{D}u_{D})^{2} + (\theta_{h}u_{h})^{2} + (\theta_{T}u_{T})^{2} + (\theta_{M_{y}}u_{M_{y}})^{2} + (\theta_{\eta_{a}}u_{\eta_{a}})^{2} =$ 1.12E + 06 Nm/m(15)

As shown in Eq. 12, Type B uncertainties are generally larger than Type A uncertainty. The Type B uncertainties generally decrease for longer wave periods, and the importance of the mass distribution becomes smaller for longer waves. This is as expected, since the monopile response becomes increasingly stiffness-dominated for long wave periods.

4.8 Total Uncertainty

The total uncertainty is a combination of both the known Type A and Type B uncertainties, (Type A uncertainty s_R and Type B uncertainty u_R). In order to combine Type A and

Type B uncertainties, the square root of the sum of squares is again used in Equation (16):

$$u_c = \sqrt{u_R^2 + s_R^2}$$
(16)

where $u_c = 1.12 \text{ E} + 06$ Nm/m, $u_R = 1.12$ E+06 Nm/m, and $s_R = 3.54$ E+04 Nm/m.

4.9 Conclusions

The uncertainty analysis suggests that Type A uncertainties (estimated through repetition tests) are of minor importance compared to



Effective Date Revision 2021 00

Type B uncertainties (estimated through a simplified analytical uncertainty propagation) for the estimation of RAOs. Based on a somewhat conservative estimate - local variation applied as a global variation - the mass and stiffness of the model itself were found to be important contributors to Type B uncertainty. The wave elevation and model diameter, where Type B uncertainties were estimated more realistically, were also seen to be important.

5. REFERENCES

- Azcona, J., Bredmose, H., Campagnolo, F., Manjock, A., Pereira, R., and Sander, F., 2014, "Methods for performing scale-tests for method and model validation", Technical report, INNWIND.EU Deliverable D4.22.
- Bachynski, E. E., Thys, M., Sauder, T., Chabaud, V., and Saether, L.O., 2016, "Real-time hybrid model testing of a braceless semi-submersible wind turbine. Part II: Experimental results", Proc. 35th Int. Conf. on Ocean, Offshore and Arctic Engineering OMAE 2016, Busan, Korea.
- Bachynski E. E., Thys, M., Delhayec V., 2019, "Dynamic response of a monopile wind turbine in waves: Experimental uncertainty analysis for validation of numerical tools", Applied Ocean Research, Volume 89, pp 96-114.
- Berthelsen, P.A., Bachynski, E. E., Karimirad, M., Thys, M., 2016, "Real-time hybrid model testing of a braceless semi-submersible wind turbine. Part III: Calibration of a numerical model", Proc. 35th Int. Conf. on Ocean, Offshore and Arctic Engineering OMAE 2016, Busan, Korea.
- Boulluec, M.L., Ohana J., Martin, A., Houmard A., 2013, "Tank testing of a new concept of floating offshore wind turbine", Proc. 32nd

Int. Conf. on Ocean, Offshore and Arctic Engineering OMAE 2013, Nantes, France.

- Det Norske Veritas, 2010, Environmental conditions and environmental loads, Tech. Rep. DNV-RP-C205.
- Gueydon, S. 2016, "Aerodynamic Damping on a Semisubmersible Floating Foundation for Wind Turbines", Energy Procedia, Volume 94, pp 367-378, ISSN 1876-6102.
- Gupta, S. and Leishman, J., 2005. "Comparison of momentum and vortex methods for the aerodynamic analysis of wind turbines", 43rd AIAA Aerospace Sciences Meeting and Exhibit (p. 594).
- ITTC, 2011, "Recommended procedures and guidelines: Seakeeping experiments", ITTC Procedure 7.5-02-07-02.1, Revision 04, 25th International Towing Tank Conference.
- ITTC, 2014a, "Guide to the Expression of Uncertainty in Experimental Hydrodynamics", ITTC Procedure 7.5-02-01-01, Revision 02, 27th International Towing Tank Conference.
- ITTC, 2014b, "General Guideline for Uncertainty Analysis in Resistance Tests", ITTC Procedures 7.5-02-02, Revision 02, 27th International Towing Tank Conference.
- ITTC, 2017, "Guideline to Practical Implementation of Uncertainty Analysis", ITTC Procedures 7.5-02-01-07, Revision 00, 28th International Towing Tank Conference.
- ITTC, 2017a, "Floating Offshore Platform Experiments", ITTC Recommended Procedures 7.5-02-07-03.1, Revision 02, 28th International Towing Tank Conference.
- ITTC, 2017b, "Model Tests for Offshore Wind Turbines", ITTC Recommended Procedures



Effective Date Revision 2021 00

7.5-02-07-03.8, Revision 01, 28th International Towing Tank Conference.

- JCGM, 2008, "Evaluation of measurement data – Guide to the expression of uncertainty in measurement", JGCM 100:2008 GUM 1995 with minor corrections, Joint Committee for Guides in Metrology, Bureau International des Poids Mesures (BIPM), Sèvres, France.
- Jonkman J., 2007, "Dynamics Modeling and Loads Analysis of an Offshore Floating Wind Turbine," Technical Report NREL/TP-500-41958, (November 2007).
- Jonkman J., Butterfield S., Musial W., Scott G., 2009, Definition of a 5-MW reference wind turbine for offshore system development, Tech. Rep. NREL/TP-500-38060, National Renewable Energy Laboratory (February 2009).
- Jonkman J., 2010, Definition of the floating system for Phase IV of OC3, Tech. Rep. NREL/TLP-500-47535.
- Jonkman J, Musial W., 2010, Offshore code comparison collaboration (OC3) for IEA Wind Task 23 offshore wind technology and deployment, Tech. Rep. NREL/TP-5000-48191, National Renewable Energy Laboratory.
- Qiu, W., Sales Jr, J., Lee, D., Lie, H., Magarovskii, V., Mikami, T., Rousset, J.-M., Sphaier,

S., Tao, L., Wang, X., 2014, "Uncertainties related to predictions of loads and responses for ocean and offshore structures", Ocean Engineering, Vol 86, pp. 58 – 67.

- Robertson, A.N., 2017. "Uncertainty analysis of OC5-DeepCwind floating semisubmersible offshore wind test campaign", (No. NREL/CP-5000-68035). National Renewable Energy Lab.(NREL), Golden, CO (United States).
- Sauder, T., Chabaud, V., Thys, M., Bachynski, E. E., and Saether, L.O., 2016, "Real-time hybrid model testing of a braceless semisubmersible wind turbine. Part I: The hybrid approach", Proc. 35th Int. Conf. on Ocean, Offshore and Arctic Engineering OMAE 2016, Busan, Korea.
- Sarpkaya T., Isaacson M., 1981, Mechanics of wave forces on offshore structures, Van Nostrand Reinhold.
- Steen, S., 2014, "Experimental methods in Marine Hydrodynamics", Lecture note, NTNU, Trondheim, Norway.
- Urban A. M., Guanche R., 2019, "Wind turbine aerodynamics scale-modeling for floating offshore wind platform testing", Journal of Wind Engineering & Industrial Aerodynamics 186 (2019) 49–57.